Answers to Items from Problem Set 1

ltem	1
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Identify the scale of measurement most appropriate for each of the following variables. (Use A = *nominal*, B = *ordinal*, C = *interval*, D = *ratio*.)

a. ____response latency (i.e., the elapsed time between being exposed to a stimulus and responding to that stimulus)

D (ratio), there is a TRUE zero point.

b. ____motivation measured by scores on the XYZ Motivation Inventory

C (interval), the trait being measured (motivation) is continuous, but there is no TRUE zero point. Usually scores on tests are assumed to be interval.

c. ____political party affiliation (Democrat, Republican, Independent, Other)

A (nominal or categorical).

d. ____academic rank in high school

B (ordinal), ranking implies ordinarily.

e. ____scores on the SAT or GRE

C (interval), again, scores on tests are usually assumed to be interval.

f. ____grade point average

Usually treated as C (interval), but probably makes better sense to treat it as B (ordinal).

g. ____responses to a Likert-type item.

B (ordinal)

h. _____the sum (or average) of responses to Likert-type items.

C (interval)

Item 2. Identify the independent and dependent variables in each of the following experiments.

	Independent	Dependent
a. students are taught	Type of	Test
statistics either with or	Teaching	Scores
without a textbook and test		
scores of the two groups are		
subsequently compared		
b. ratings of self-confidence	This is a correlational study, there are no	
are found to be correlated	independent or dependent variables	
with high school		
c. fifteen minutes a day	Type of	Number
practicing shooting 3 point	practice	of 3-point
goals proved more effective	proved more effective goals	
than thirty minutes of practice		
twice a week		

ltem 3

Use the following sets of data to compute the values requested

Data (X): 9 12 13 14 15 16 16 17 18 20

Data (Y): 2 1 0 -1 2 2 -2 1 0 1

Answer

ΣX = 150
$\Sigma X^2 = 2340$
$(\Sigma X)^2 = 22500$
$\Sigma X + 2 = 152$
$\Sigma(X+2) = 170$
$\Sigma(X+2)^2 = 2980$
Σ2X = 300
$\Sigma 2X + 2 = 302$
$\Sigma 2(X+2) = 340$
ΣΧΥ = 83
ΣXY + 2 = 85
$\Sigma(X+2)(Y+2) = 435$
ΣX/N = 15

$\Sigma X^2 / N = 234$
ΣXY/N = 8.3
$\Sigma X \Sigma Y = 900$
Σ6y = 36
Σ 6y = 36 5 Σ y = 30
<i>'</i>

Using a table of areas under the normal curve, compute the following:

- a. the proportion of cases below a z-score of -.72.
- b. the proportion of cases below a z-score of 1.65.
- c. the proportion of cases above a standard score of 2.0.
- d. the proportion of cases above a standard score of -2.5.
- e. the proportion of cases between z-scores of -1.5 and 1.5.
- f. the proportion of cases between standard scores of 1.5 and 2.5.

To answer these, we need the **Table of Areas Under the Normal Curve** given in any introductory statistics textbook. Also, we need to remember that the table gives (1) the area (or **proportion**) of cases between the mean and the **absolute** value of a given standard score (**z-score**) and (2) the proportion of cases greater than the absolute value of a specified z-score.

a. In the table, the proportion of cases between the mean and a z-score of .72 is .2642. Since we are working, here, with a **negative** z-score we note, first, that the proportion of cases below the mean is .5. Since the proportion of cases between the mean and a z-score of -.72 is .2642, we subtract .2642 from .5, yielding .2358, the proportion **below** a z-score of -.72.

A easier way to have obtained this answer is to use the area **beyond** the z-score. Of course, in this case, since z is negative, the area beyond gives the proportion **below** a z-score of -.72. Reading directly from the table, the area beyond a z-score of .72 is .2358. Hence the proportion of cases below a z-score of -.72 is .2358.

 b. Here, we need to remember that the table only gives proportions for half the normal distribution. Looking up a z-score of 1.65 we find that the proportion between the mean and 1.65 is .4505. To this we must add the proportion below the mean (.5). Adding the two proportions gives .9505. Hence 95.05% of the cases in a normal distribution fall below a z-score of 1.65.

Assuming a normal distribution with a mean (μ) = 50, and a standard deviation (σ) = 10, using a table of areas under the normal curve, compute the following. (Note, you can find a table of areas under the normal curve in just about any introductory statistics book. You can find a table of areas under a normal curve, HERE, also.)

a. the proportion of cases below a score of 42.

b. the proportion of cases below a z-score of .66.

c. the proportion of cases above a score of 70.

d. the proportion of cases above a score of 25.

e. the proportion of cases between of 35 and 65.

f. the proportion of cases between scores of 65 and 75.

- Note, first, that a score of 42 converts to a z score of (42-50)/10 = -.8. Using a table of areas under a normal curve, we find that proportion between the mean a a z of .8 is .2881. Since our z is -.8 we need to subtract .2881 from .5, or .2119.
- b. The proportion of cases between the mean (i.e., z score of 0) and a z score of .66, according to a table of areas, is .2454. Since .5 of the cases are already below a z score of 0, we need to add this to the .2454. Thus, we find that .7454 of the cases are below a z score of .66.
- c. .0228
- d. .9938 (Hint: This is the sum of .4938 and .5)
- e. .8664 (Hint: This is 2 x .4332)
- f. .0606 (This can be obtained either by using the area between the

mean and z, [.4938 - .4332] or the area beyond z, [.0668 - .0062].

ltem 5

Assume the mean on an IQ test is 100 with a standard deviation of 16. Using a table of areas under the normal curve, estimate each of the following:

To answer these, we need the formula for a standard (z) score. Recall that this is:

$$Z = \frac{\left(X - \overline{X}\right)}{s}$$

Where

X = the score, $\overline{X} =$ the mean of the distribution, and s = the sandard deviation.

a. Find the percentage of individuals having an IQ of 130 or higher.

First compute the z-score

z = (130-100)/16 = 30/16 = 1.875 (round to 1.88).

Then look up the **proporton in tail** (Column C) for a z-score of 1.88. The proportion is .0301. Hence, about 3% have IQs of 130 or higher.

b. Find the proportion of individuals with an IQ of 90 or lower.

z = (90 - 100)/16 = -10/16 = -.625

According to the Unit Normal Curve Table (Appendix B), the proportion **in the tail to the left** (hence, below, Column C) a z-score of -.62 is .2676. Hence, a little less than 27% of the individuals have IQs lower than 90.

c. Find the percentage of individuals with IQs between 85 and 115.

The z-score for an IQ of 115 is .94 (*rounded from .9375*); the z-score for an IQ of 85 is -.94.

The area to the left (below) a z-score of .94 is .8264 (Column B).

The area to the left (below) a z-score of -94 is .1736 (Column C).

Hence the proportional area between -.94 and .94 is the *difference*

between the two proportions (.8264 - .1736) or .6528.

d. Find the proportion of individuals with IQs between the first and third quartiles.

The first and third quartiles correspond the the 25th and 75th percentiles, respectively. Furthermore, percentiles are directly related to proportions (or areas) of a normal distribution: .25 (or 25%) of the distribution lies below the 25th percentile; .75 (or 75%) lies below the 75th percentile. Hence .5 lie between the 25th and 75th percentile.)

e. Find the percentage of individuals with IQs above 130.

An IQ score of 130 corresponds to a z-score of 1.875 (or 1.87).

Using Column C in the Unit Normal Curve Table we see that the proportion *above* a z of 1.87 is .0397.

Hence, approximately 4% of individuals have IQ scores above 130.

f. Find the IQ of individuals at the 85th percentile.

An individual at the 85th percentile has a *z*-score of 1.04 (Note: since the 85th percentile is *above the median* we use Column B and scan down until we find .8508. The corresponding to *z*-score is 1.04).

Now, solve the z-score equation for X:

 $X = Zs + \overline{X}$

Then compute, X = 1.04(16) + 100 = 116.64, or, after rounding to the nearest whole score, an IQ of 117.

g. Find the IQ of individuals at the 35th percentile.

35% of the distribution lies **below** the 35th percentile. We can use the Table of Unit Normal Curve Table to determine that this corresponds to a z-score of -.38 (*using Column C*).

Next, using the formula above to solve for X, we obtain,

X = -.38(16) + 100 = 83.36, or an IQ of 94.

ltem 6

A survey of 1,000 kindergarten children reveals that the average child watches 145 minutes of TV per week. The uncorrected *sample* standard deviation is 40 minutes. Construct the 95% confidence to estimate the mean number of minutes spent viewing TV per week in the *population* of kindergarteners.

We have the sample size (1000) and the sample standard deviation (40). To compute the confidence interval we need the **standard error of the mean (***SEM***)**:

$$SEM = \frac{s}{\sqrt{(N-1)}}$$
$$= \frac{40}{\sqrt{999}}$$
$$= \frac{40}{31.607}$$
$$= 1.266$$

The 95% confidence interval is then given by:

$$\begin{array}{l} 95\%\,CI = \overline{X} - 1.96(SEM\,) \leq \mu \leq \overline{X} + 1.96(SEM\,) \\ \\ = \overline{X} - 2.481 \leq \mu \leq \overline{X} + 2.481 \\ \\ = 142.52 \leq \mu \leq 147.48. \end{array}$$

We conclude, 95% confidence, that the **true** mean number of minutes children spend watching TV per week is somewhere between 142.52 minutes and 147.48 minutes per week.

a. Is it important that Schmalling first examine the *reliability* of her new instrument? Explain your reasoning.

Yes, it is important that she first establish the reliability the instrument. If the instrument is not reliable, then scores on the instrument reflect error (noise or random responding), in which case not valid inferences can be drawn.

b. What type of evidence for validity was Schmalling looking for? What results would provide evidence instrument is valid?

Schmalling was looking for construct (convergent-divergent) evidence of validity. She hoped for a reasonably strong correlation between scores on the new instrument and scores on the *Attitude Toward Mathematics* instrument (since the two instruments presumably assess similar characteristics) and a relatively weak correlation between scores on the new instrument and scores on the *Motivations for Reading* instrument (since attitudes and interests in reading is, presumably, independent of attitudes and interests in mathematics).

Item	Item 8							
	The table below shows the number of students, classified by age and whether or not a parent had attended college, over a 10-year period, who attained an Associate's Degree from a local community college.							
	a.	What is the probability o student who is 28 years o	-	ociate's Degre	ee for a			
	b. What is the probability of attaining an Associate's Degree for a first-generation student who is 23 years old?							
	c. Of the six combinations (of age and parent attendance) which group has the highest probability of attaining an Associate's Degree?							
		Number of Students A	Attaining an Ass	ociate's Deg	ree by			
		Parent College Atter	ndance Status a	nd Age Cate	egory			
				Age Category	/			
	Status of at least one parentLess than 2525 to 35Greaterattended collegeyrs oldyrs old35 yrs							
	Parent	t attended college	1252	1215	632			
	No pa	rent attended college	643	736	592			
a. b.	1951/5	bility of an Associate's Deg 5106 = .38. bility of attaining an Associ		·				

student who is 23 years old = 643/5106 = .13.

c. Highest probability of attaining an Associate's Degree = Less than 25 yrs old whose parents attended college: prob. = 1252/5106 = .256.

ltem 9

A school district dietitian wants to construct a confidence interval to estimate the mean number of soft drinks high-school students consume daily in her district. She intends to survey the students. Assuming a *population* standard deviation of 1.8 soft drinks a day,:

- a. how many students must she survey in order to obtain a 95% confidence interval that is .5 soft drinks wide?
- b. how many students would she have to survey to obtain a 99% confidence interval that is .5 soft drinks wide?

A 95% confidence interval that is .5 wide is obtained when the interval,

$$\mu = \overline{X} \pm 1.96(SEM)$$

is .5 wide. This occurs when,

1.96(*SEM*)

is equal to .25 (half on either side of the mean). Hence, solving for the SEM gives

$$SEM = \frac{.25}{1.96} = .1276.$$

We use this value and the equation for SEM $\left(=\sqrt{\sigma^2/(N-1)}\right)$ to solve for N. We have,

$$SEM^{2} = \sigma^{2} / (N-1)$$
, or

$$.0163 = \frac{3.24}{(N-1)}$$
. Solving for N

$$(N-1) = \frac{3.24}{.0163} = 198.77.$$

So that, when rounded up, N = 199.

A 99% confidence interval that is .5 wide is obtained when the interval,

$$\mu = \overline{X} \pm 2.58(SEM)$$

is .5 wide. This occurs when,

2.58(*SEM*)

is equal to .25 (half on either side of the mean). Hence, solving for the SEM gives

$$SEM = \frac{.25}{2.58} = .0969.$$

Using logic identical to that used for computing the N needed for 95% CI, we arrive at (N-1) = 344.681. Hence, we would need a sample size of 346.

The distribution of SAT-V scores is assumed to be normal with μ = 500 and σ = 100.

a. What is the *probability* of someone having an SAT-V score *higher* than 650?

b. What is the *probability* of an SAT-V score *between* 550 and 650?

Probabilities are associated with areas under the normal curve. Think of the TOTAL area under the normal curve as being equal to 1. Then portions of this area give probabilities.

The distribution of SAT-V scores is normal with m = 500 and s = 100.

a. What is the *probability* of someone having an SAT-V score *higher* than 650?

First convert the SAT-V score of 650 to a *z*-score of 1.5.

Then, using Column C in the Unit Normal Curve Table, find that the proportion, .0668, lies *above* a *z*-score of 1.5. Hence, the probability of an SAT-V score above 650 in .0668 (or, after rounding, .07).

b. What is the *probability* of an SAT-V score *between* 550 and 650?

Again, using *z*-score transformations and the Unit Normal Curve Table, we find that a proportion of .9332 lies *below* a *z*-score of 1.5 and that a proportion of .6915 lies *below* a *z*-score of .5 (the *z*-score associated with an SAT-V score of 550).

The difference between these two proportionis (.9332 - .6915) is .2417. Since proportions can be read as probabilities, the probability of an SAT-V score *between* 550 and 650 is .24 (rounded).

he correlation between SAT scores and first semester GPA in the general population is about .53. What do you suppose is the correlation between SAT and GPA at Harvard? Will it higher, lower, or about the same? Explain your reasoning.

The correlation will be lower (probably close to zero), because Harvard admits a highly selected group of freshmen. Most of them would be expected to have very high GPAs and to score very high on the SAT. Hence, Harvard's freshmen should exhibit a very narrow range (i.e., very little variance) of both SAT scores and GPSs.

The correlation between two variables, x and y is given by

$$r_{xy} = \frac{s_{xy}}{\sqrt{s_x^2 \times s_y^2}}$$

where S_{xy} is the *covariance* between x and y, and S_x^2 and S_y^2 are, respectively the *variances* of x and y. Because of the highly restricted range of both x and y, the correlation between them is *attenuated*.

The mean GRE score for a sample of 121 students who completed a GRE preparation course was 1030 with a corrected standard deviation of 175. The national mean GRE score is 1000. Is this difference statistically significant? Do you think the difference is practically significant? Explain your reasoning.

Compute a one-sample t test, where t = (1030-1000)/SEMSEM = SD_{Corrected}/sqrt(N) = 175/sqrt(121) = 175/11 = 15.9091 t = 30/15.9091= 1.886 The critical value of t at $\alpha = .05$ with 120 degrees of freedom is 1.98. Hence, the t is not statistically significant. Since t is not statistically significant, it

cannot be practically significant.

13. Using the dataset below set up an SPSS database and run the following descriptive analyses: gender, ethnicity, and score. Also, create a graphic display (of your choice) that explains the data. Export all SPSS output into Word.

Be sure to label all values so the output is readable and clear. Data is listed in order for each subject (gender, ethnicity, grade).

1) 1, 3, 75

- 2) 1, 4, 98
- 3) 2, 6, 90
- 4) 1, 4, 85
- 5) 1, 6, 88
- 6) 2, 4, 90
- 7) 2, 1, 94
- 8) 2, 1, 83
- 9) 1, 1, 75
- 10) 1, 4, 70

Gender: 1=female; 2=male

Ethnicity: 1=African American; 2=American Indian; 3=Asian; 4=Caucasian; 5=Hispanic; 6=Multiracial

Answer:

	Statistics							
I	gender ethnicity score							
		Valid	10	10	10			
	N	Missing	0	0	0			
	Mean		1.40	3.40	84.80			
	Median		1.00	4.00	86.50			
	Mode		1	4	75 ^a			

a. Multiple modes exist. The smallest value is shown

gender							
		Frequency	Percent	Valid Percent	Cumulative		
					Percent		
	female	6	60.0	60.0	60.0		
Valid	male	4	40.0	40.0	100.0		
	Total	10	100.0	100.0			

ethnicity							
	Cumulative						
					Percent		
	African American	3	30.0	30.0	30.0		
	Asian	1	10.0	10.0	40.0		
Valid	Caucasian	4	40.0	40.0	80.0		
	Multiracial	2	20.0	20.0	100.0		
	Total	10	100.0	100.0			



Item 14. Using the data set below, conduct an independent-samples ttest examining the differences between Cohort 18 (18) and Cohort 19 (19) on exam scores.

Is there a significant difference between the two groups? Produce SPSS output and write a p value statement to indicate your answer.

1)	99	18
2)	80	18
3)	65	18
4)	50	18
5)	88	18
6)	90	18
7)	80	18
8)	61	18
9)	77	18
10)	70	18
11)	90	19
12)	92	19
13)	85	19
14)	84	19
15)	71	19
16)	90	19
17)	60	19
18)	86	19
19)	83	19
20)	71	19

Answer:

The means of Cohort 18 and Cohort 19 did not differ significantly, p = 3.75.

	Group Statistics								
Cohort N Mean Std. Deviation Std. Error Mea									
	ExamScores	Cohort 18	10	76.00	14.757	4.667			
	Examocores	Cohort 19	10	81.20	10.422	3.296			

Independent Samples Test							
		e's Test for v of Variances		or Equality of Means			
		F	Sig.	t	df		
	Equal variances assumed	1.076	.313	910	18		
ExamScores	Equal variances not assumed			910	16.189		

Independent Samples Test

		t-tes	t for Equality of M	leans
		Sig. (2-tailed)	Mean Difference	Std. Error Difference
	Equal variances assumed	.375	-5.200	5.713
ExamScores	Equal variances not assumed	.376	-5.200	5.713

Independent Samples Test

		t-test for Equality of Means				
		95% Confidence Interval of the Difference				
		Lower	Upper			
ExamScores	Equal variances assumed	-17.203	6.803			
	Equal variances not assumed	-17.300	6.900			

Item 15. Using the data set below, conduct a paired-samples t-test examining the differences between pre- and post-exam scores.

Is there a significant difference between the two groups? Produce SPSS output and write a p value statement to indicate your answer.

nd writ	te a p v	/alue st
1)	9998	
2)	8087	
3)	6577	
4)	5077	
5)	8885	
6)	9096	
7)	8089	
8)	6189	
9)	7780	
10)	70	90
11)	90	88
12)	92	98
13)	85	98
14)	84	98
15)	71	89
16)	90	98
17)	60	59
18)	86	89
19)	83	92
20)	71	90

Answer:

The means of Exam 1 and Exam 2 did differ significantly, p < .05, p = .000.

		Mean	Ν	Std. Deviation	Std. Error Mean
Pair 1	ExamScores1	78.60	20	12.717	2.844
	ExamScores2	88.35	20	9.588	2.144

Paired Samples Statistics

Paired Samples	Correlations
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		Ν	Correlation	Sig.
Pair 1	ExamScores1 & ExamScores2	20	.698	.001

Paired Samples Test

	Paired Differences			
	Mean	Std. Deviation	Std. Error Mean	95% Confidence Interval of the Difference Lower
Pair 1 ExamScores1 - ExamScores2	-9.750	9.136	2.043	-14.026

Paired Samples Test

	Paired Differences	t	df	Sig. (2-tailed)
	95% Confidence Interval of the Difference			
	Upper			
Pair 1 ExamScores1 - ExamScores2	-5.474	-4.773	19	.000